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# Laser Guiding and Wakefield Acceleration In Plasmas



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Physics Department Qualifying exams



Work in collaboration with:

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# Laser pulse in a plasma excites a wake field

An intense laser pulse of length  $L \sim \lambda_p/2 = \lambda c/\omega_p$  in a plasma excites a copropagating electron plasma wave  $\rightarrow$  laser wakefield

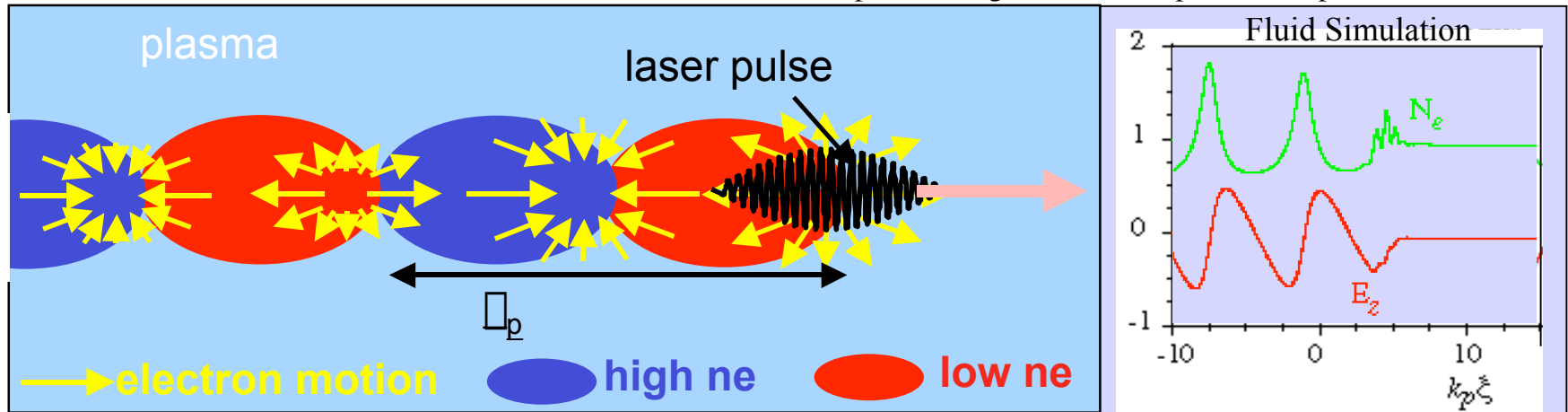
-electrons are ejected from a intense pulse by pondermotive pressure

$$V_{\text{pond}} = mc^2 a_0^2 / 4e \quad \text{where} \quad a_0 = eE / \hbar mc$$

resulting from oscillation of the electrons in the spatially varying laser field

-in the wake of the pulse electrons rush back in a time  $\lambda/\omega_p$

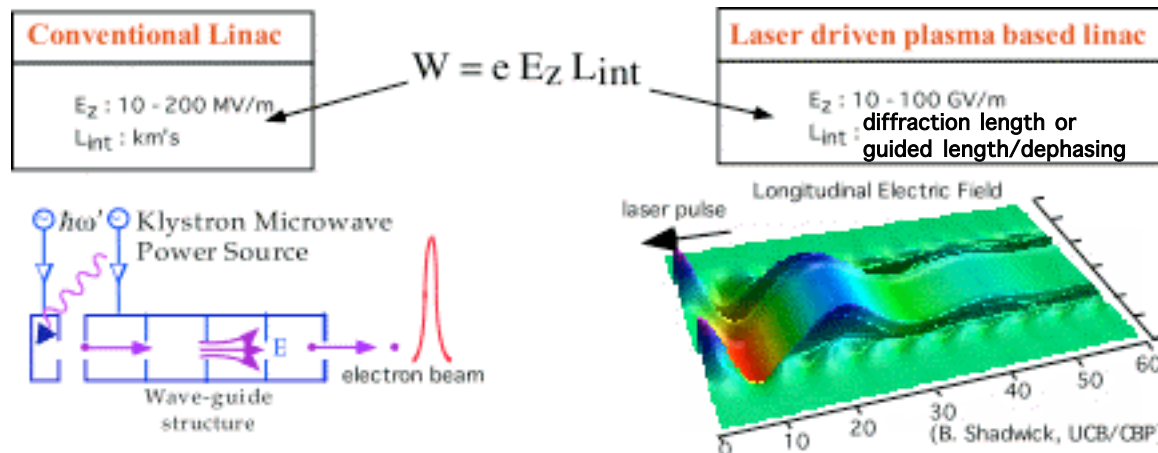
-if pulse length is matched to this time, an electron plasma wave follows in the wake of the pulse with  $v_{\text{phase}} = v_{g, \text{laser}}$  &  $\omega_{\text{peak}} \sim \omega_p$



-Linear regime is  $\sim$  sinusoidal: density depletion and  $n_{e, \text{min}} \rightarrow 0$  distorts  
Longer pulses can self modulate at  $\omega_p$  and also self guide  $\rightarrow$  simple accelerator but without control.



# Laser driven plasma based linacs offer high gradients



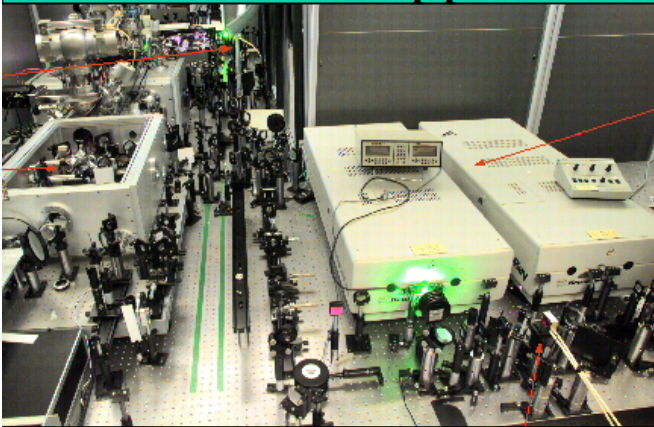
- Plasma wave excitation using high intensity multi TW laser pulses offers
  - High gradient: limited by wavebreaking  $eE/m\omega \sim \omega/k$ .  $\sim 100 \text{ GeV/m} @ 10^{18}/\text{cm}^3$  (50fs)
  - Short wavelength structure  $\lambda_p = 2\pi c/\omega_p \sim 40 \mu\text{m} @ 10^{18}/\text{cm}^3$
  - High phase velocity  $\sim \omega_{g,laser} = \omega_p/\omega = 50 @ 10^{18}/\text{cm}^3$
- Key issues:
  - Production of wakes, acceleration, optimization
  - Injection of electrons
  - Laser guiding: extend acceleration length beyond diffraction
  - Coupling to structure & Dephasing - control of density & gradient
  - Staging



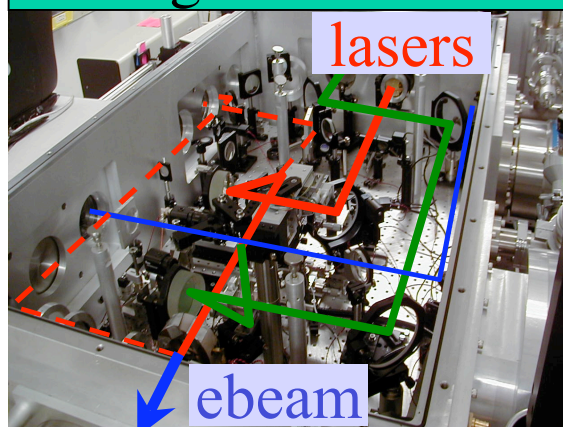
# Laser driven accelerator R&D at l'OASIS lab

- Test bed for R&D concepts towards 1 GeV module of a laser accelerator
- Facility includes 10 TW, 50 fs laser system @ 10 Hz (100 TW under development)
- Comprehensive diagnostics & control systems

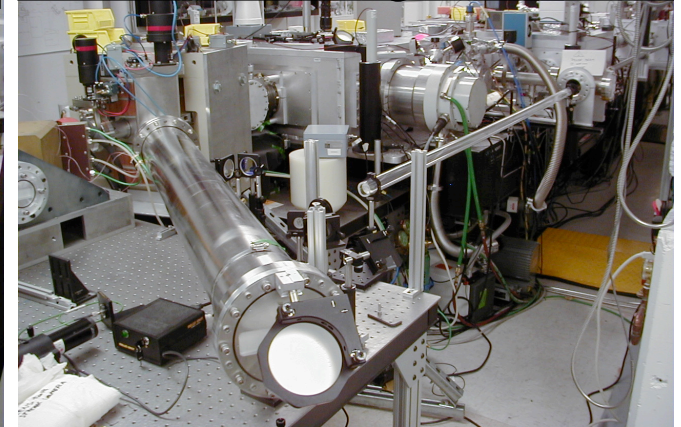
## 10 TW Ti:sapphire



## Target Chamber



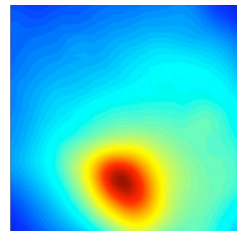
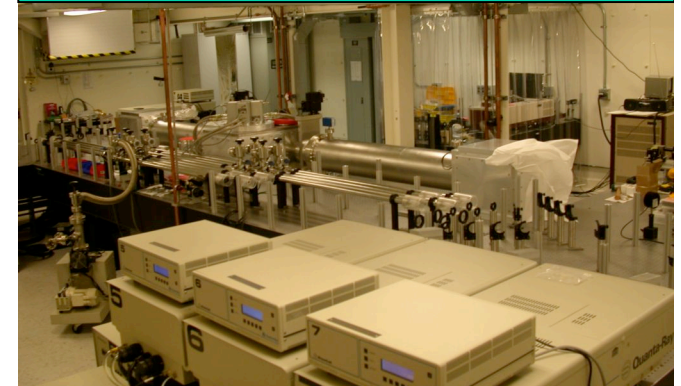
## Shielded target room



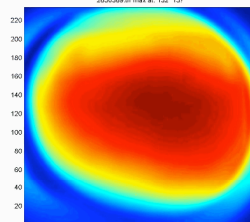
## Control Room



## 100 TW Ti:sapphire Under construction



High energy  
< 10 mrad



Low energy  
100 mrad





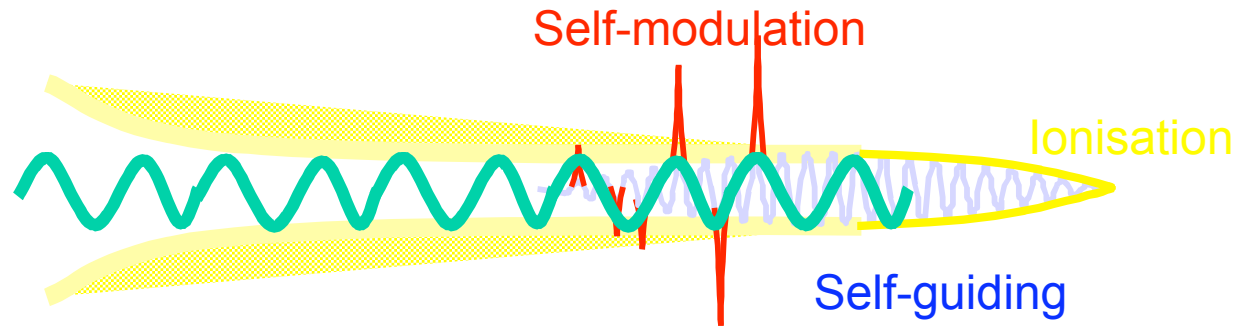


# Thesis Topic: Laser Guiding and Wakefield Acceleration in Plasmas

- Experimental study of wakefield acceleration focusing on the effects of laser guiding, electron injection, and plasma tuning.
  - First guiding of acceleration relevant intensities ( $>10^{18}\text{W/cm}^2$ ) over many  $Z_R$
  - Demonstration of controlled injection into wakefield accelerator
  - Characterization of plasma effects on acceleration
- Preliminary and development experiments (in progress)
  - Self modulated laser wake field (SMLWFA) experiments  
*Leemans et al, PRL 2002 ; Leemans et al., Phys. Plasmas 2001*
  - Gas target modeling and development
  - Laser, Control and diagnostic development  
*Geddes et al, Proceedings of AAC 2002 ; Leemans et al., Phys. Plasmas 2001*
- Main experiments (beginning fall 02)
  - Laser guiding via plasma channel @  $I > 10^{18}\text{W/cm}^2$   
*Volfbeyn et al, Phys. Plasmas 1999*
  - Controlled injection & Guiding in standard wakefield (LWFA) experiments
    - Colliding pulse injection - *Esarey et al, PRL 1997*
    - SMLWFA Injectors - *Reitsma et al, PRST-AB 2002*
  - Guided self modulated experiments



# SM-LWFA experiments produce $>1\text{nC}$ electron bunches with significant fraction at $>25\text{MeV}$



## Self-modulation occurs when:

- Power  $>$  Critical power
- Laser pulse length  $\gg$  Plasma period

## Then

- Pulse self guides
- Pulse modulates into pulses @  $\lambda_p$

## Currently Available:

- Power = 2.5 - 10 TW, pulse length = 60-15  $\mu\text{m}$
- With plasma density  $n_e = 3 \times 10^{19} \text{cm}^{-3}$  self modulation when:
- $P > 1 \text{ TW}$
  - Laser pulse length  $\gg 6 \mu\text{m} = \lambda_p$

## Experiments scan:

- target density and position
- laser pulse length/chirp

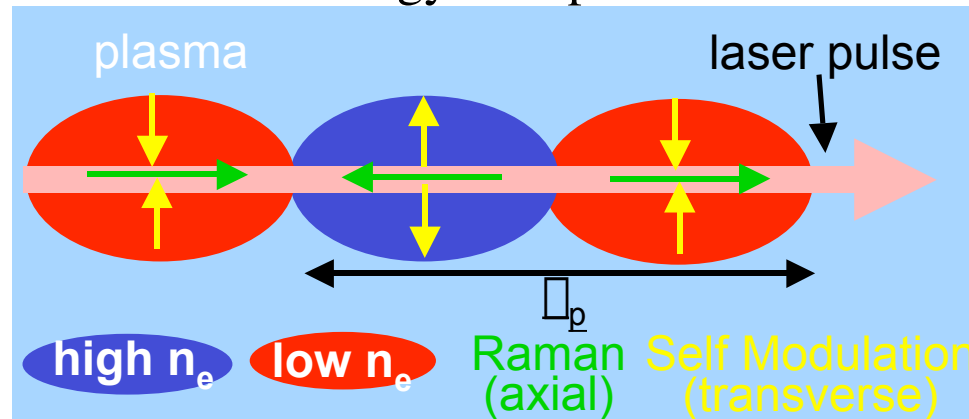
## Observe:

- Plasma density and profile
- Laser pulse shape
- Beam charge, collimation
- Beam energy from nuclear activation, magnetic spectrometer
- Transmitted light spectrum



- $$1 - \frac{p^2}{2n^2} = 1 - \frac{p^2}{2n^2} (1 + a^2)^{1/2}$$

- Wake driven up from noise by forward Raman scattering(1d) and Self Modulation(2d).  
Small initial perturbation -> energy transport & enhanced wake/ modulation

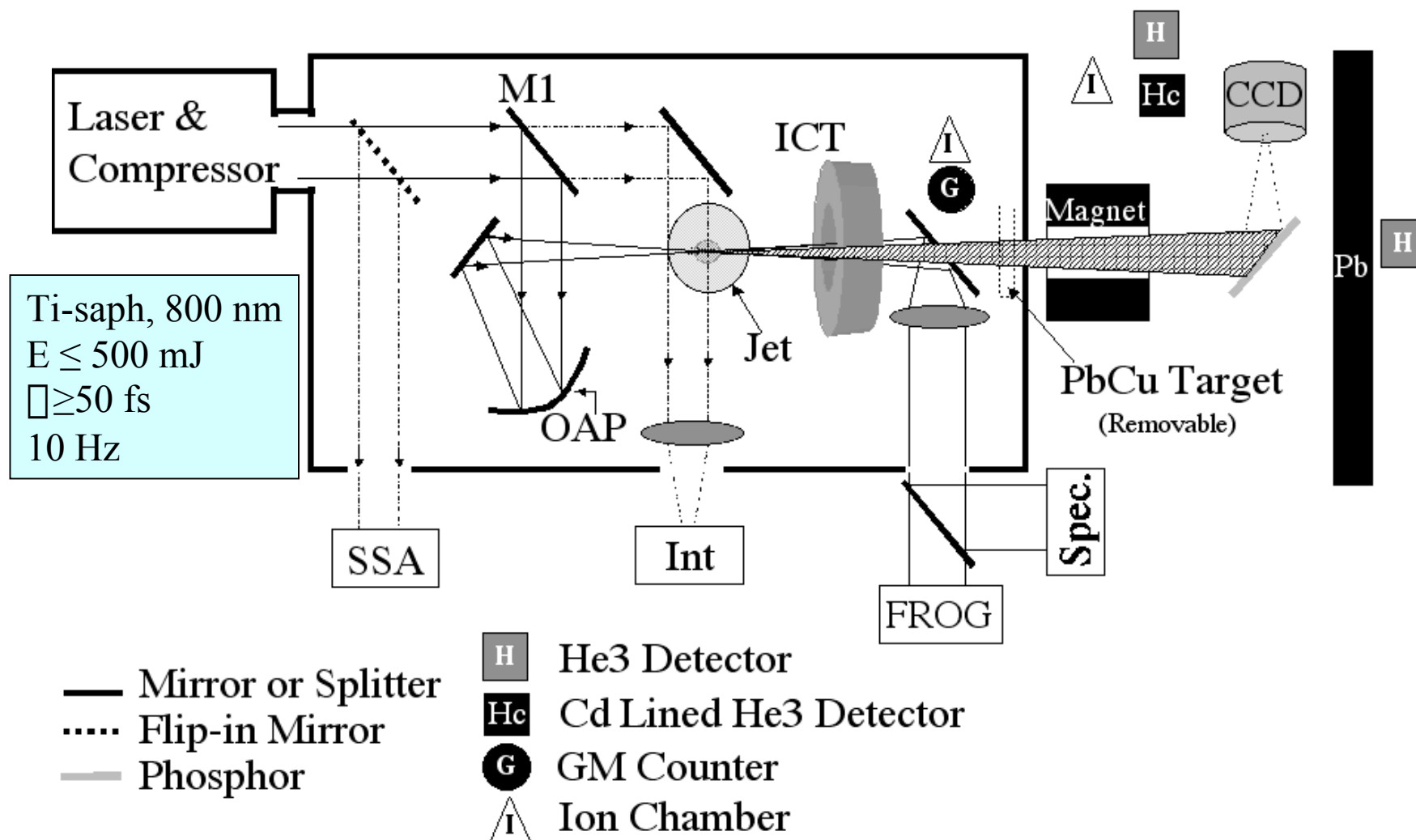


- Particles are trapped by Raman backscatter (slow beat wave) or wave breaking
- Simple, single beam experiment
- High charge due to high density
- Low energy due to low  $\gamma$  and 100% energy spread due to uncontrolled injection





# Experimental set-up at the 10 TW, 10 Hz l'OASIS laser

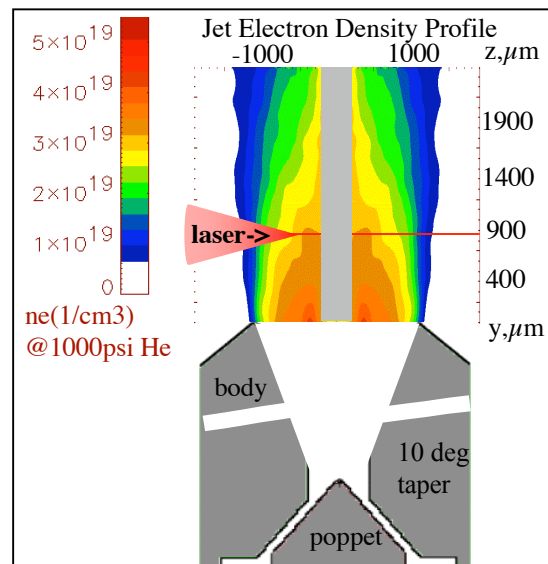
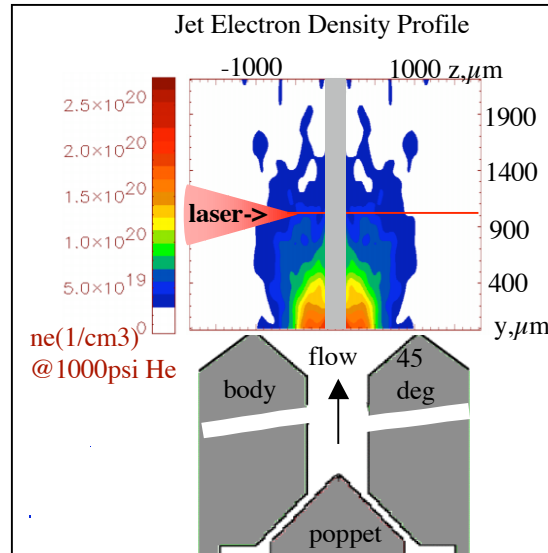
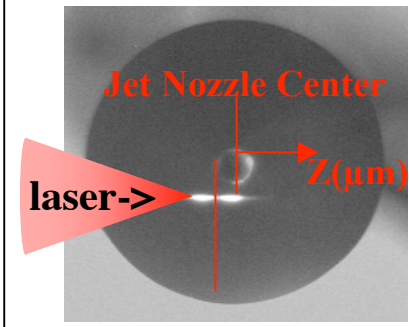


\*W.P. Leemans et al., Phys. Plasmas 2001

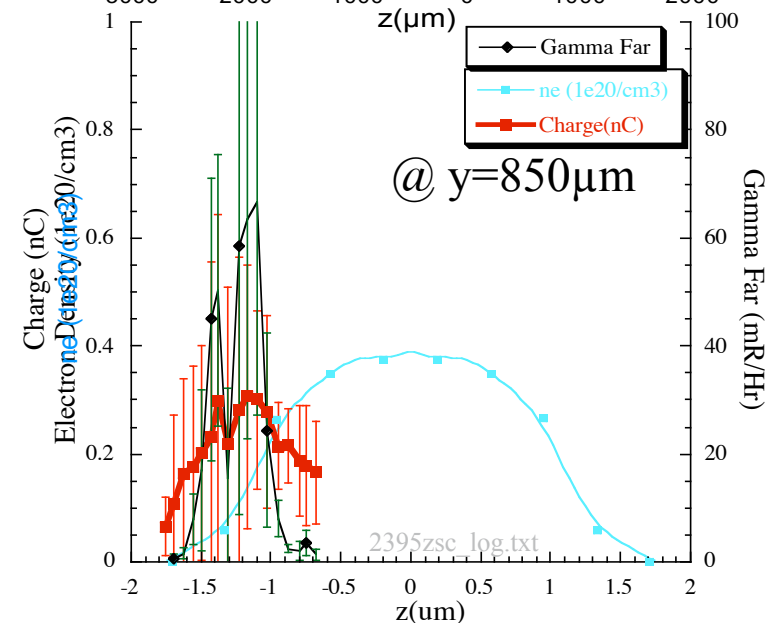
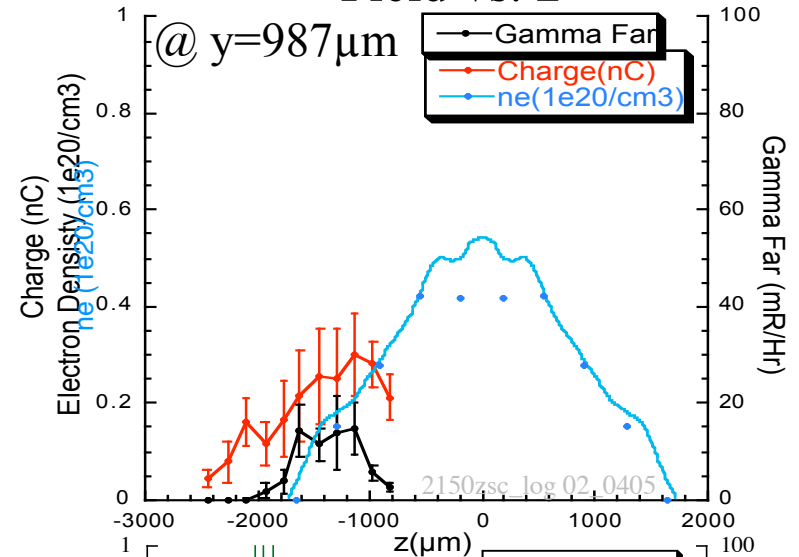


# Jet optimization is under way to control and enhance accelerator output

Top view of jet showing geometry



Yield vs. z

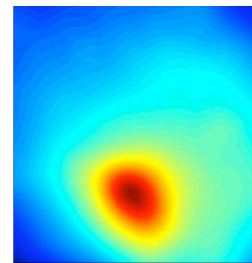
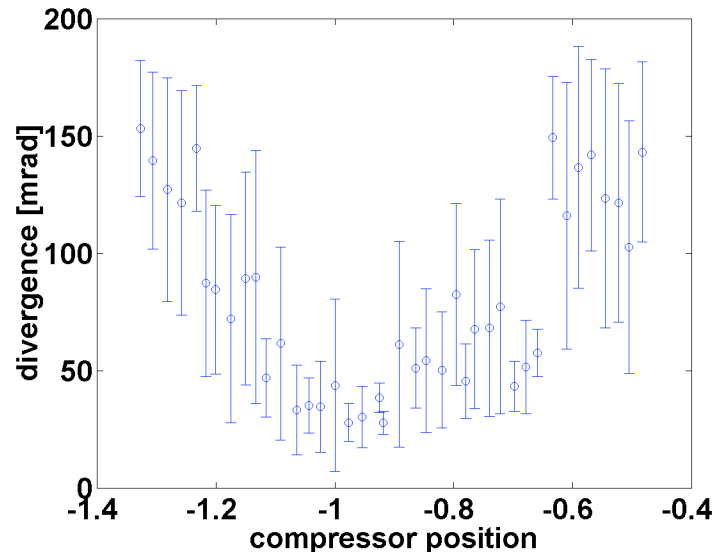




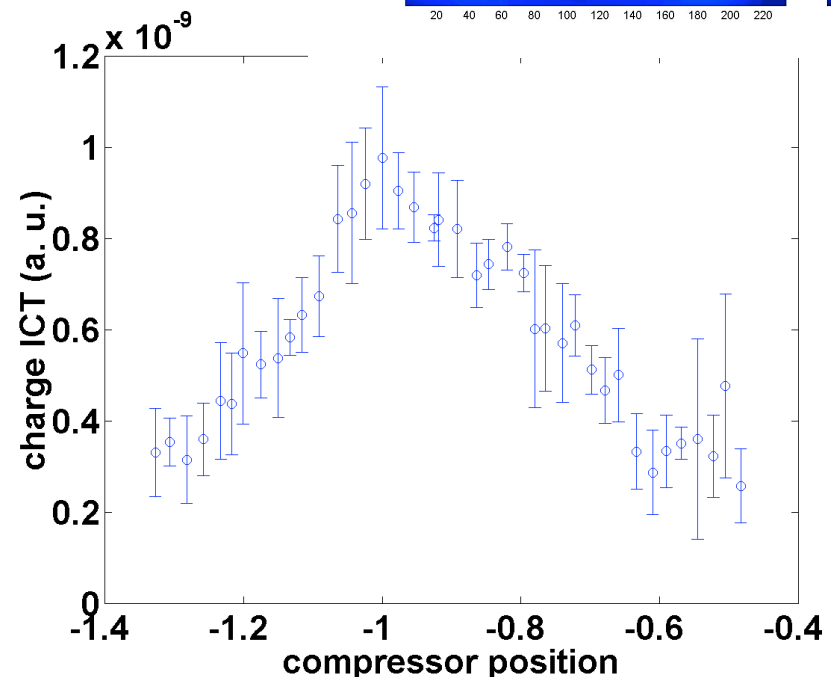
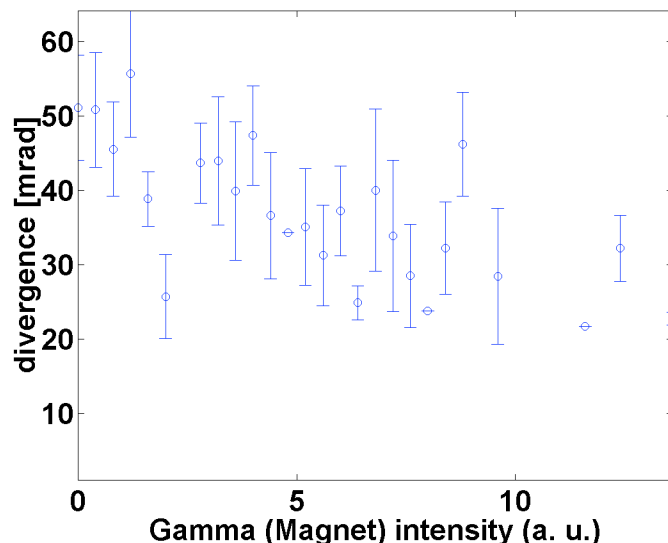
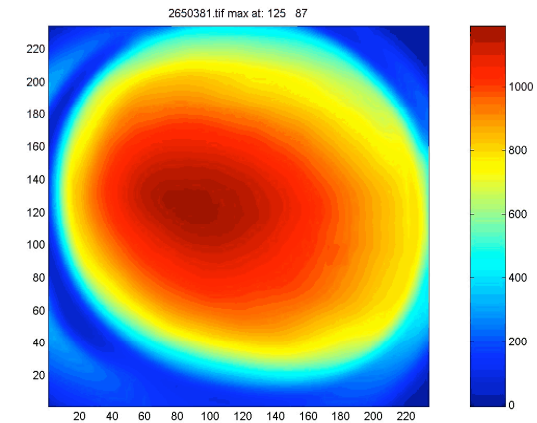
# Divergence reduces to 10mrad at high peak power

## Characterization & modeling of beams under way

E-beam on phosphor screen, 75 cm away



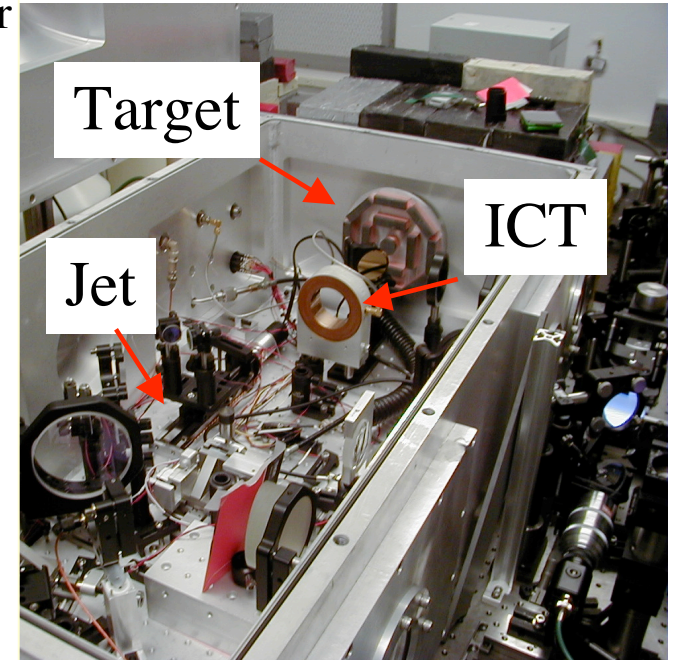
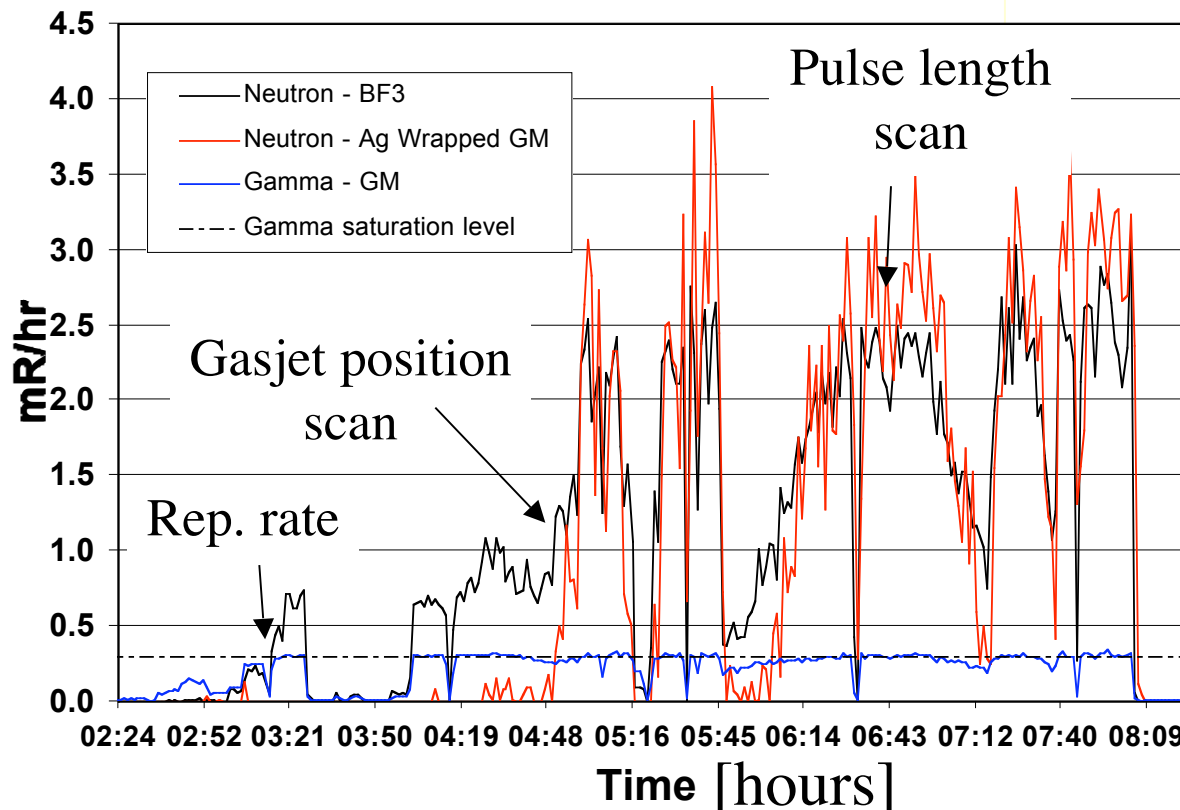
10 mrad





# Nuclear activation measurements show electron beam energy >25 MeV and demonstrate radioisotope production

- Observed  $\text{Cu}^{63} (n, \gamma) \text{Cu}^{64}$  activity > 0.5  $\mu\text{Ci}$  in < 1/2 hr  
=> Beam energy > 25 MeV
- Observed  $\text{Na}^{24}$  from  $\text{Al}^{27}$   
=>  $(n, \gamma)$  reaction i.e. >6 MeV neutrons
- Control electron & neutron yield with laser/plasma
- > 3 mR/hr neutron yield



->Beam energy measurement

->Isotope production experiments funded

->need to increase  $e^-$  fraction >25MeV





# Further Self Modulated Experiments Planned

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- steep gradients appear beneficial
- 5x increase in gamma ray yield for equal  $q_{\text{bunch}}$
- need to
  - Better characterize beam:  
Magnetic spectrometer & beam phosphor on line.
  - Do detailed experiments with sidescatter diagnostic to characterize spot evolution and repeatable laser performance for various nozzles
  - Make new nozzles for steeper profiles
  - Understand ionization effects: Pre ionized experiments are now possible with multi beam set up.
  - model beam propagation to understand effect of different gradients
    - SDE analytic model (Esarey et al)
    - WAKE quasi static 3D PIC



# Nozzle & Valve Optimization is Important for Accelerator Performance

- Gas jets used in wake field experiments to overcome ionization induced refraction
- Accelerator performance depends critically on jet density, profile, and smoothness as well as on laser focus location in the jet.
- Jet optimization is likely to significantly improve performance.
- Anticipated optimal conditions include:
  - densities of  $10^{18}$  to  $10^{19}$  (achieved)
  - gradient scale lengths of  $\sim Z_R \sim 100\text{-}200\mu\text{m}$  (currently  $0.5 - 1\text{mm}$ )
  - density fluctuations  $< 5\%$  (unknown)
  - cm scale slit jets to allow long  $L_{\text{int}}$  and colliding pulse
  - faster gas pulses (short on-time allows high rep rate with low pump load)
  - shaped density profiles to escape detuning (long term)
- Jet development efforts include:
  - design and testing of new nozzle shapes (cylindrical and asymmetric)
  - advanced machining to allow production of novel nozzle shapes
  - development of new valve technologies (PZT, micro valves)
  - 2w asymmetric imaging interferometer in the accelerator chamber
  - (coming year) modeling of accelerator performance with various profiles



# 1d Wall Following Perfect Flow Code Allows Fast Modeling of Cylindrical & Rectangular Nozzles

Use the equations of perfect gas flow in a variable area duct derived from assuming isentropic expansion of a perfect gas:

$$T/t_0 = 1 / \left( 1 + \left( \frac{\gamma - 1}{2} \right) M^2 \right)$$

$$P/p_0 = 1 / \left( 1 + \left( \frac{\gamma - 1}{2} \right) M^2 \right)^{\gamma / (\gamma - 1)}$$

$$\rho / \rho_0 = 1 / \left( 1 + \left( \frac{\gamma - 1}{2} \right) M^2 \right)^{1 / (\gamma - 1)}$$

$$A/A^* = (1/M) * \left( \frac{2}{1 + \gamma} \right) * \left( 1 + \left( \frac{\gamma - 1}{2} \right) M^2 \right)^{(\gamma + 1) / (2 * (\gamma - 1))}$$

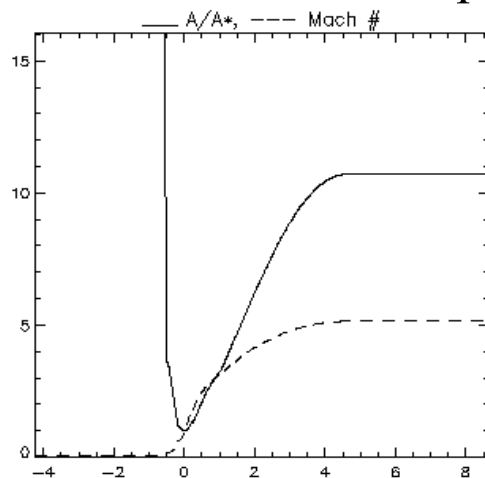
Calculate flow direction at each z location by assuming linear variation of flow angle over cross section & using midpoint.

Allows fast optimization of nozzle shape for smooth mach # contour with cylindrical or slit valves

Includes effects of flow direction due to poppet & throat shape.

Geometry export to CMC codes & 3d flow simulations

## Example Output



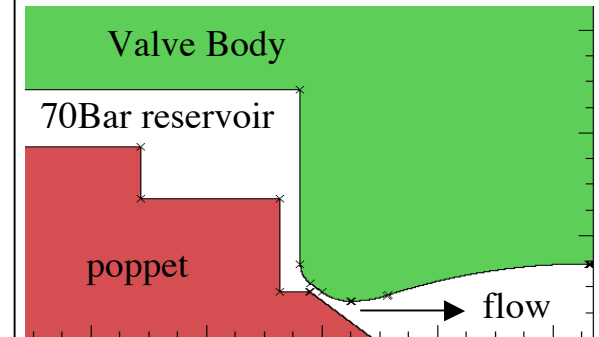
06- GV bell nozzle redesign  
Mon Aug 27 17:20:26 2001

Throat Data:  
At=0.619303, Zt=-0.00384712

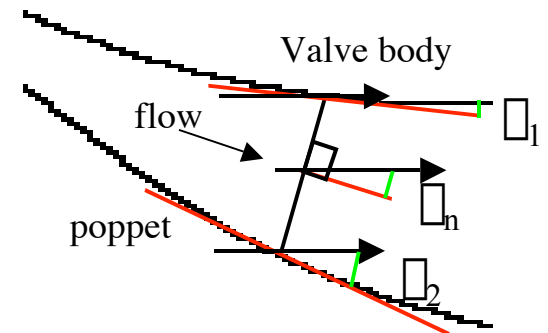
Opening & poppet data:  
opening distance=0.193507, z(open)=-0.00384712  
poppet area=2.56647, flow area at opening=0.619303  
M at opening=1.00001, Max pressure=77.9281

Outflow Data:  
Ae/A\*=10.7017 Ae=6.62758, Re=1.45248  
Me=5.14001, RhomaxE=1.33768e+20, RhoE/rho0=0.0317880

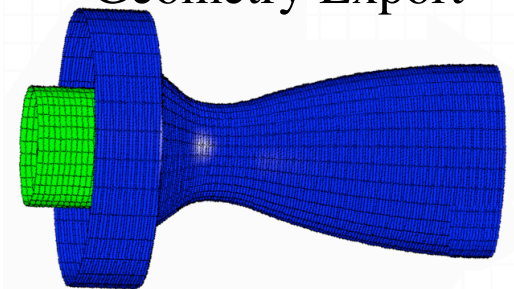
## Nozzle Illustration (half)



## Code Geometry Illustration



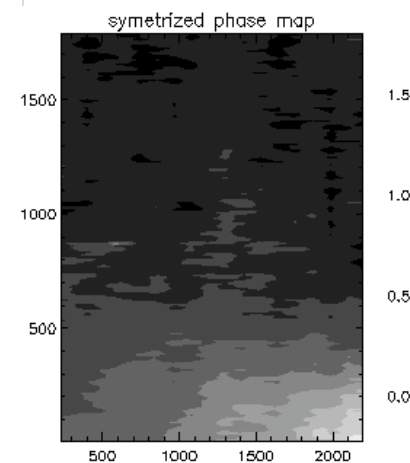
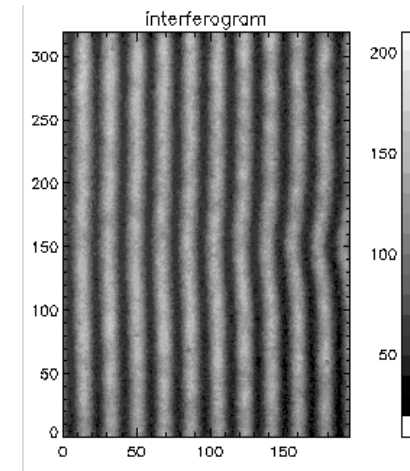
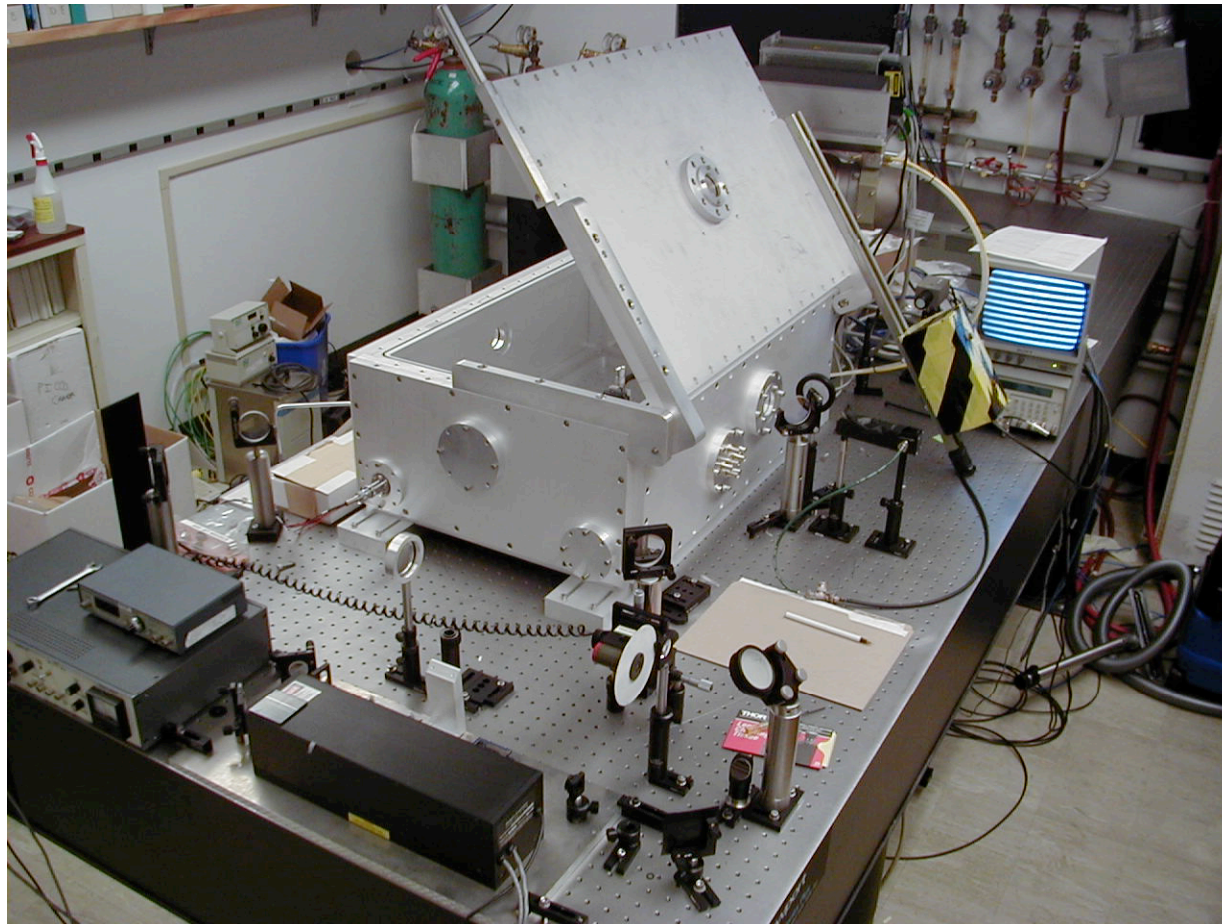
## Geometry Export



Collaboration with Petersson, LLNL



## Test stand with HeNe neutral density interferometer allows fast characterization of nozzles



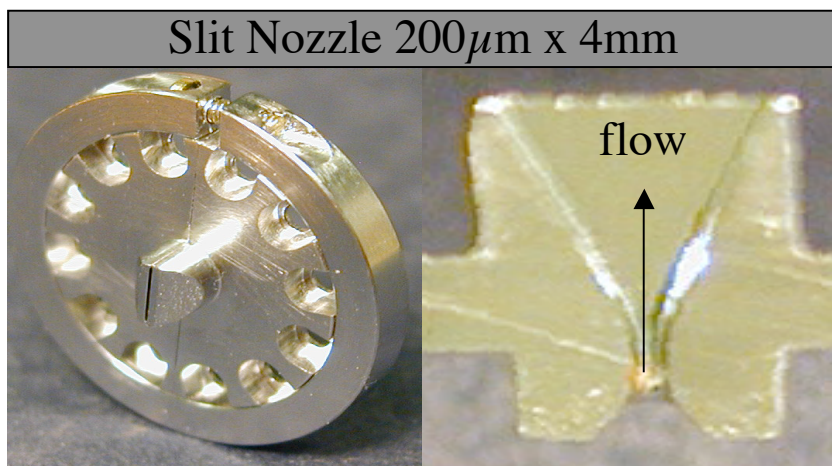
- Neutral density interferometer & fringe tracing recovers 2d phase map with  $\sim 0.1$  rad resolution
- Benchmarked against plasma interferometer
- Testing of nozzles on solenoidal gas jets is under way
- Quick feedback allows rapid iteration of shapes



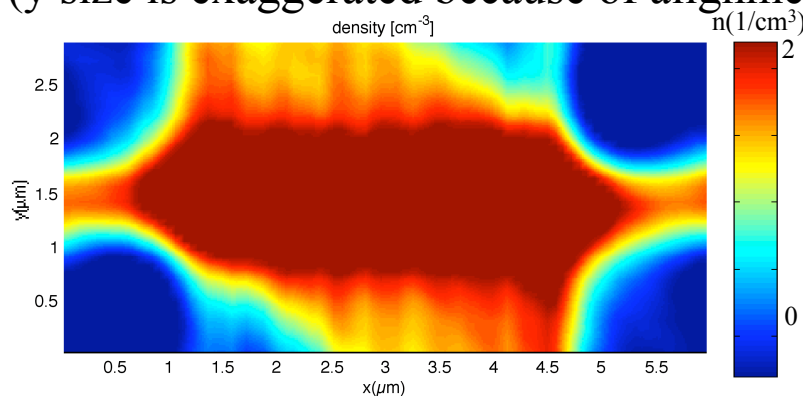


## Advanced nozzles and drivers are under development

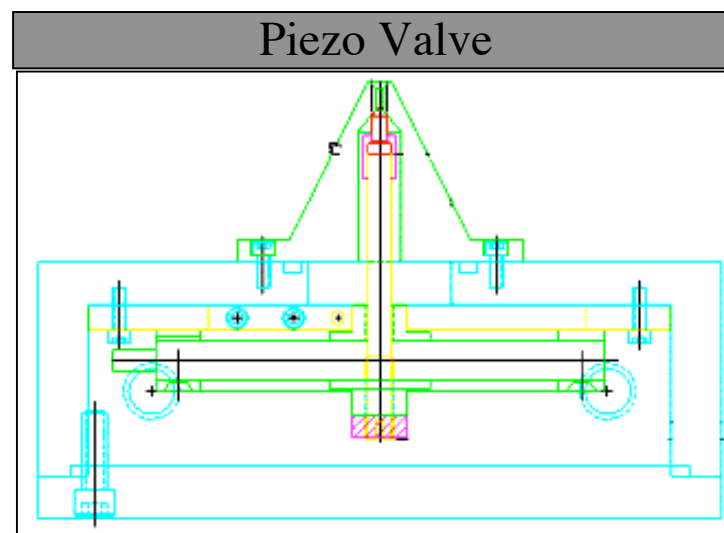
- Slit nozzles not possible with traditional techniques made using computer machining
- Important for injection experiments



Preliminary Density 1mm from nozzle  
(y size is exaggerated because of alignment)



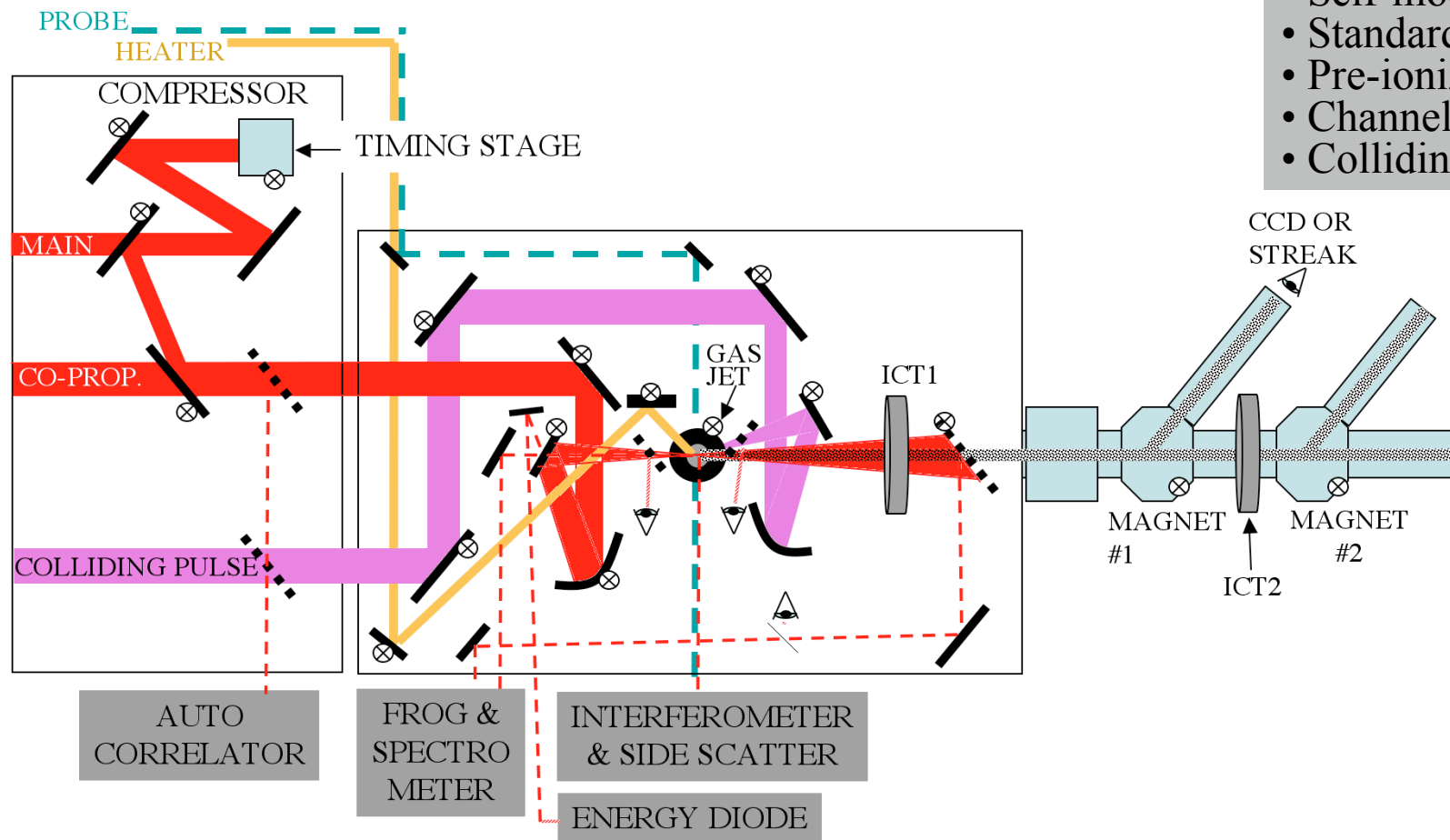
- PZT driven valve built and being tested.
- Faster response & greater force than solenoid valves
- Higher rep rate, lower pump loads, and larger opening areas for long jets.





# Target area and laser bay have been upgraded to accommodate multiple beam experiments

- Experiments:
- Self-modulated
  - Standard LWFA
  - Pre-ionized
  - Channel Guide
  - Colliding pulse



KEY:   
 - - - - - PROBE/DIAGNOSTIC BEAMS (DASHED)   
 ——— MAIN BEAMS (SOLID)   
 ..... ELECTRON BEAM (DOTS)

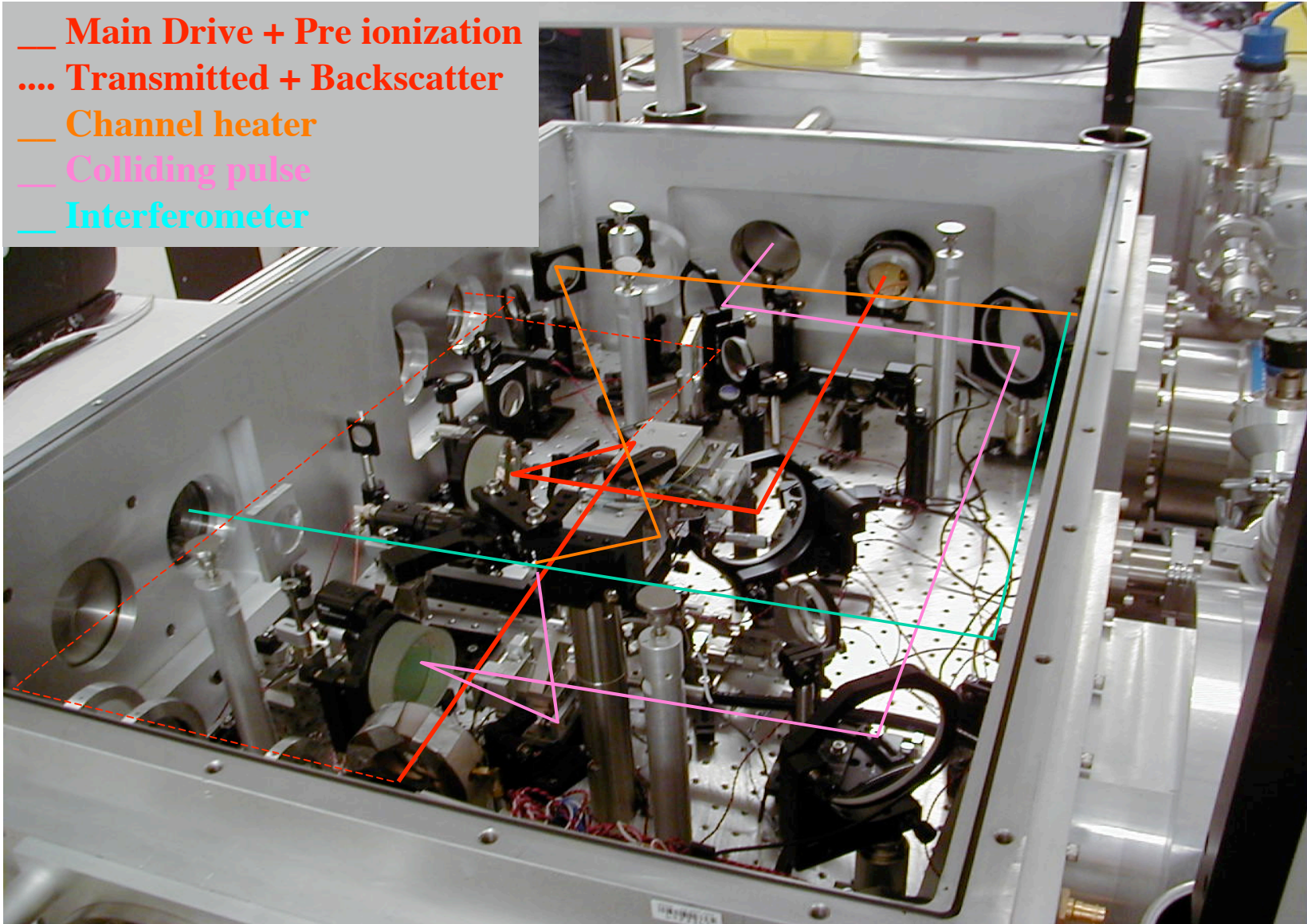
DIAGNOSTICS   
 ▼ CAMERAS

⊗ CONTROL POINTS   
 - - - - - FLIP IN MIRROR



# Target area and laser bay have been upgraded to accommodate multiple beam experiments

- Main Drive + Pre ionization
- ... Transmitted + Backscatter
- Channel heater
- Colliding pulse
- Interferometer



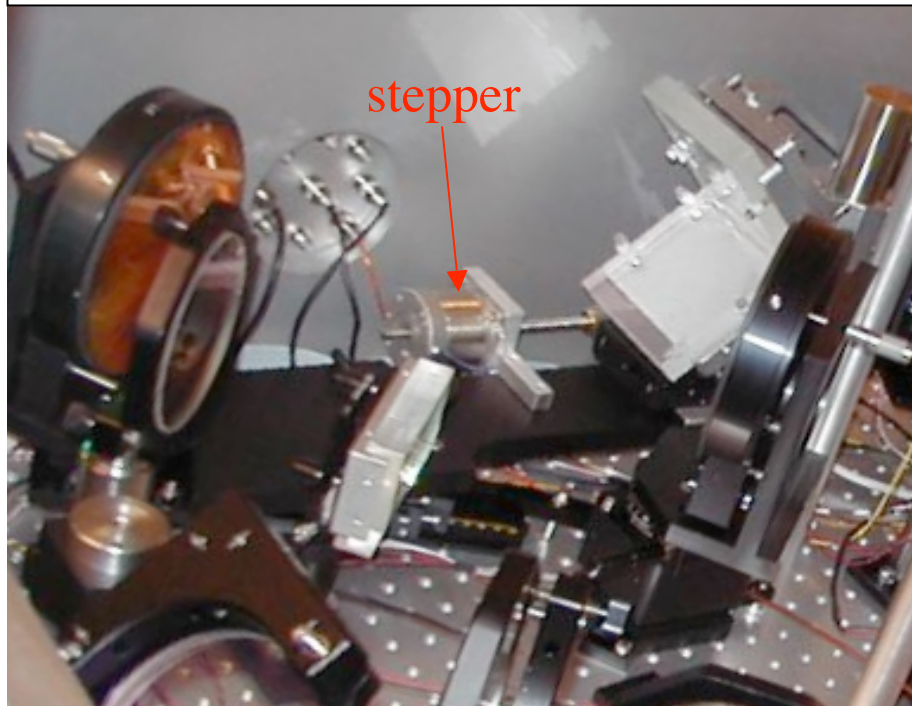




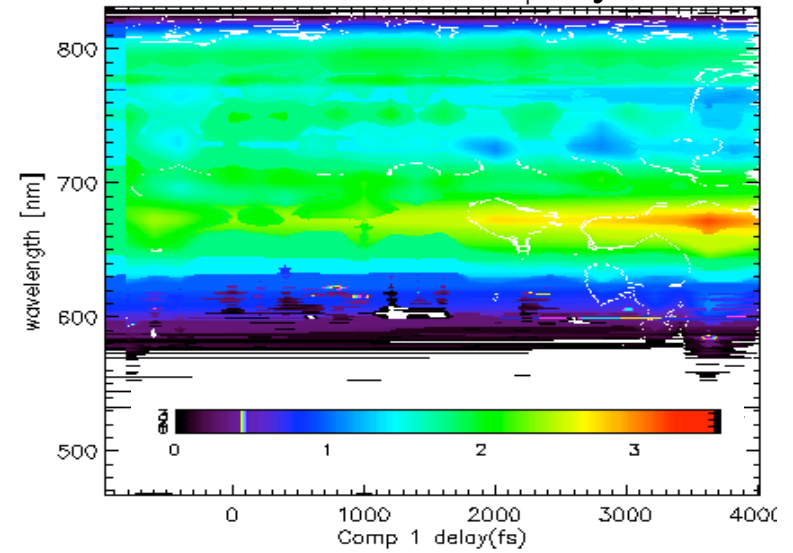
# Timing system has been installed

- Beam timing remotely adjustable with fs precision using stepper motors & remote control system
- Allows synchronization of multi beam experiments
- Compressor movement automatically compensated
- Need to characterize stability

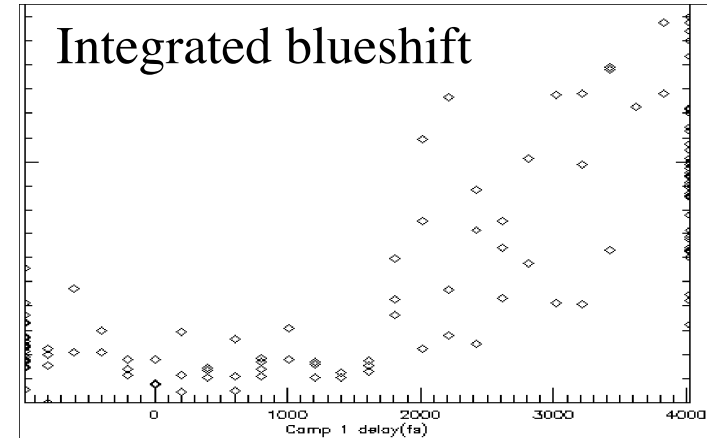
Delay stages on Compressors



Measurement of Blue Shift of Beam0 in Plasma made by Beam1 versus Beam 1 delay



Integrated blueshift



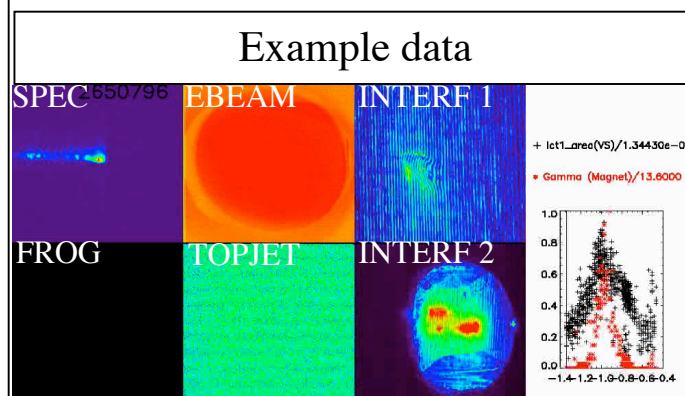
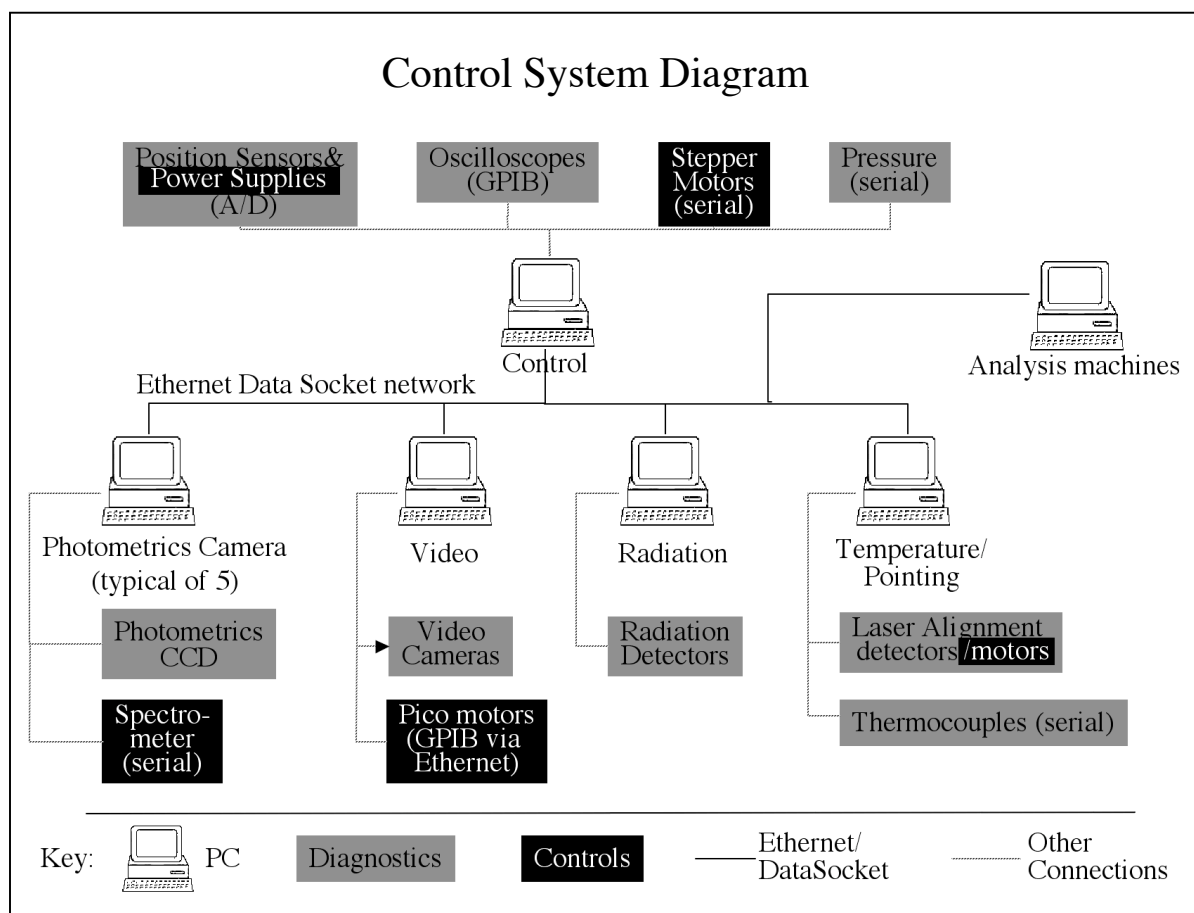




# Network based control for the l'OASIS accelerator allows collection of correlated data from diagnostics

- Experiments require collection of synchronous data at Hz rep rates
- A central control system has been implemented that uses low cost IP networking
- Sets up many remote machines and diagnostics for each shot, then saves the data
- Data is distributed on the network for viewing

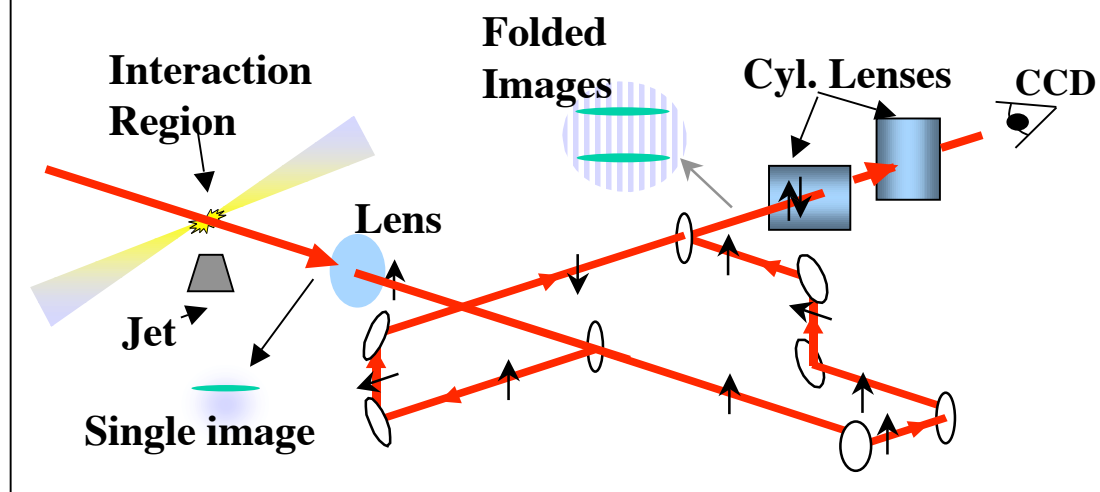
- Controls include:
- magnet current
  - beam timing, pointing
  - jet position
  - compressor position





# Asymmetric imaging camera and 2 $\pi$ interferometer measure plasma during system shots, separates sidescatter

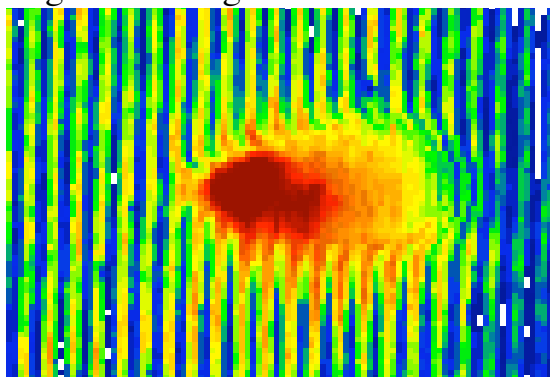
## Interferometer Setup



- Interferometer upgrade has been fielded on accelerator and is taking first data.
- 1.4mm \* 7mm asymmetric field of view allows imaging of long thin plasma channels
- Allows measurements of plasma at full system energy -> actual shot conditions

## 1 $\pi$ Symmetric imaging :500 mJ

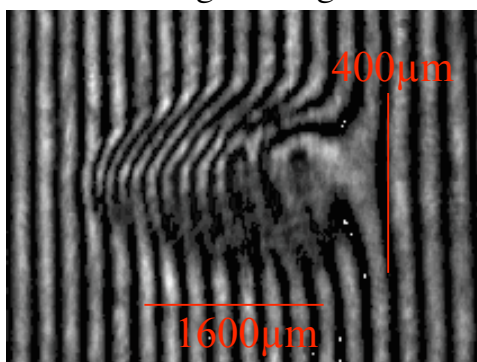
- sidescatter contaminates interferogram
- insufficient resolution
- fringe shift too great



## First images: Asymmetric 2 $\pi$ interferometer

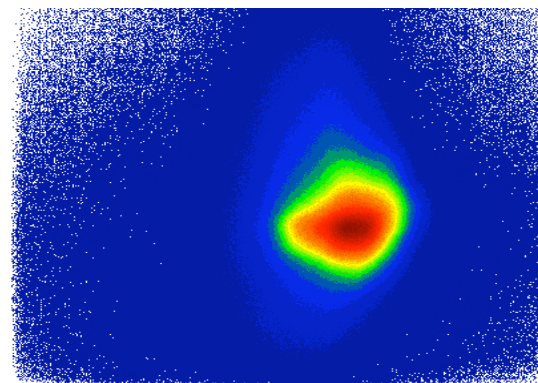
### Partial interferogram: 500mJ

- sidescatter tolerable even at high power
- resolution, fringe shift good



### Side Scatter isolated:50mJ

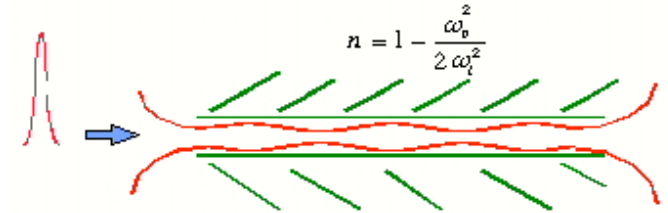
- Separate analysis possible





# Laser Guiding Extends Acceleration Region

- Acceleration occurs over distance where laser intensity remains large:  $\sim Z_R$  without guiding
- Guiding occurs due to refractive index peaked on axis. For a plasma well below critical density:



$$1 - \frac{\omega_p^2}{2\omega_l^2} = 1 - \frac{4\pi e^2 n_e(r)/m}{2(1 + a^2)^{1/2}} \approx 1 - \frac{\omega_{po}^2}{2\omega_l^2} \left(1 - \frac{a^2}{2} + \frac{\Delta n}{n} + \frac{\Delta n}{n}\right) \quad \text{for small } a \text{ \& } \omega_p$$

- For pulses  $\sim \omega_p$ , the wake density perturbation  $\Delta n$  cancels the relativistic effect  $a^2$
- Guiding by density channel  $\Delta n/n$  is required for short pulses
- Solution of wave equation with parabolic density profile shows gaussian mode of radius  $r_o$  for:

$$1 - \frac{\omega_{po}^2}{2\omega_l^2} \left(1 + \frac{\Delta n r^2}{n r_o^2}\right) \quad \Delta n = \frac{1}{\omega_e r_o^2} \quad r_{channel} \geq r_o$$

- Tunneling losses can be modeled from WKB theory, coupling from mode overlap.
- Spot evolution for unmatched beams can be modeled by SDE or paraxial wave eqn.



# Plasma Channels Guide Laser in Gas Jet

## Plasmas: Hydrodynamic Ignitor-Heater Method.

Experiments have guided  $2 \times 10^{17}/\text{cm}^2$  over several mm with  
 $>50\%$  efficiency using channels formed by hydrodynamic shock\*.

Low Z gasses are required for high intensity guiding

Two pulse formation scheme uses:

Ultrashort pulse with  $I > 10^{14} \text{ W}/\text{cm}^2$  for ionization

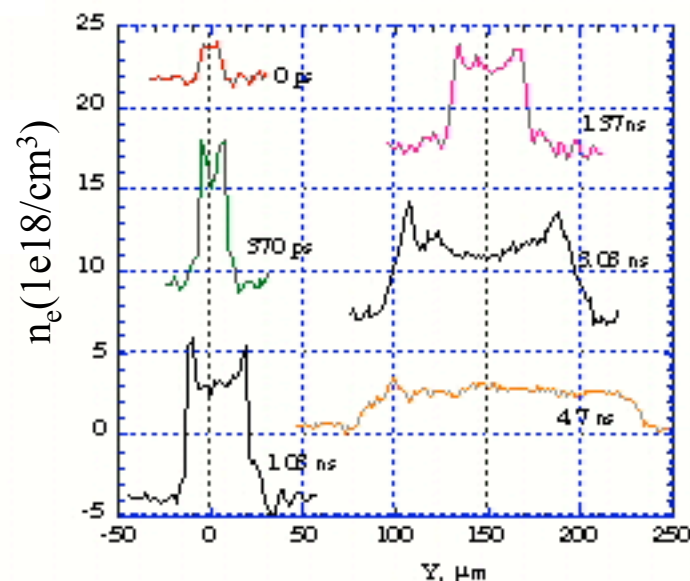
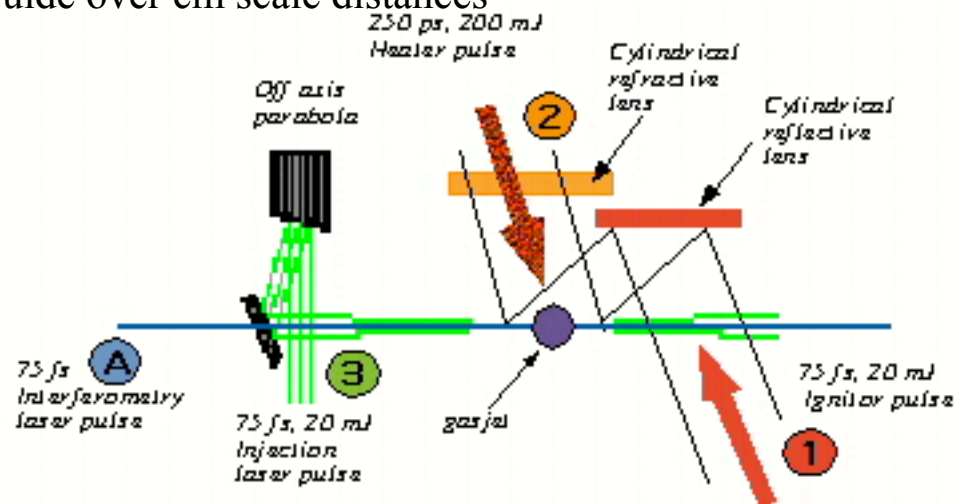
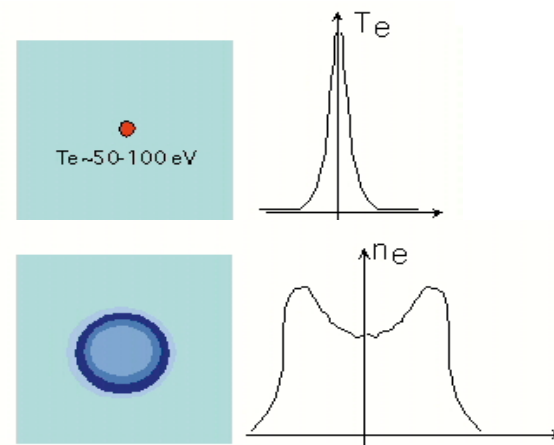
250ps pulse with  $I \sim 10^{13} \text{ W}/\text{cm}^2$  for inverse Bremsstrahlung heating

Future work:

Extend intensity of guided pulse to  $> 10^{18}/\text{cm}^2$  &  $n_e \sim 10^{18}/\text{cm}^3$

Match channel & mode to allow more efficient guiding

Guide over cm scale distances

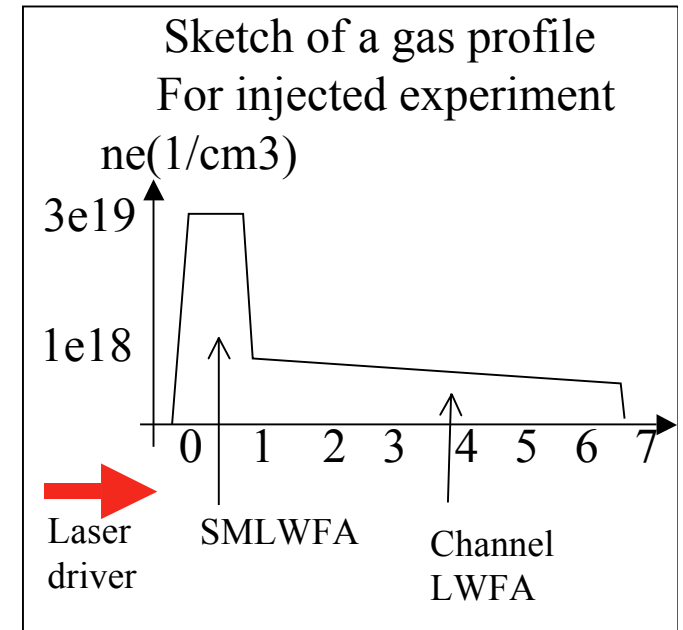


\* P. Volfbeyn, MIT Ph.D. Thesis '98  
 P. Volfbeyn and W.P. Leemans, EPAC 98  
 P. Volfbeyn, E. Esarey and W.P. Leemans, Phys. Plasmas '99

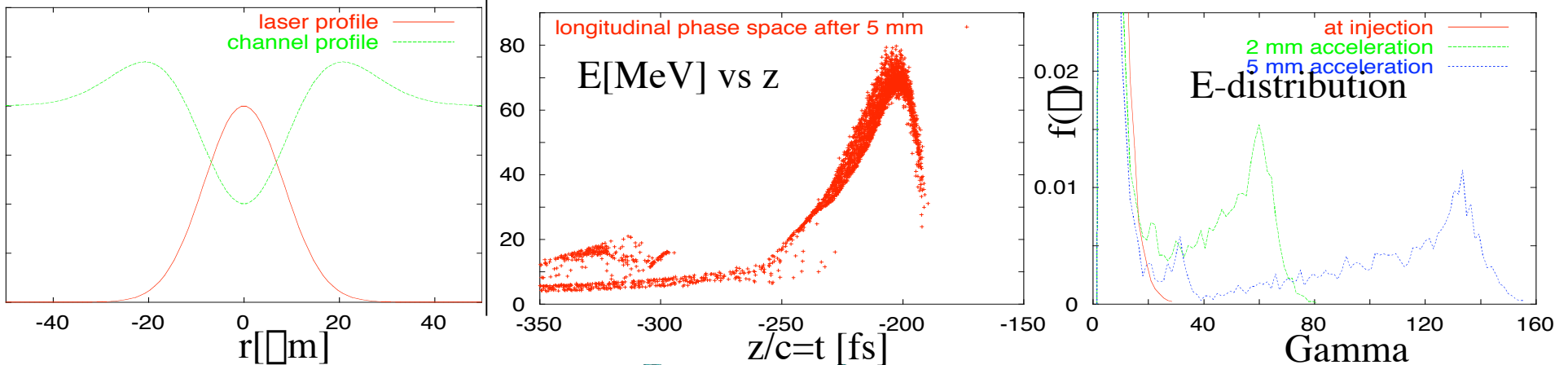


# Integrating Self Modulated injector and channel experiments: Expect $10^3$ - $10^4$ (n) yield increase

- Non linear fluid code\* shows that bunches from a self modulated accelerator can be trapped and accelerated by a channel guided wakefield accelerator
- Simple injection mechanism
- High charge, narrowed distribution: few hundred pC above 30MeV (increase of  $10^4$ )
- Suitable for radio isotope production
- Challenges:
  - Channel guided accelerator
  - close coupling to self modulated accelerator
  - staging using same or separate beams



\*Ref: A. Reitsma, et al., PRST-AB,5, 051301 (2002)

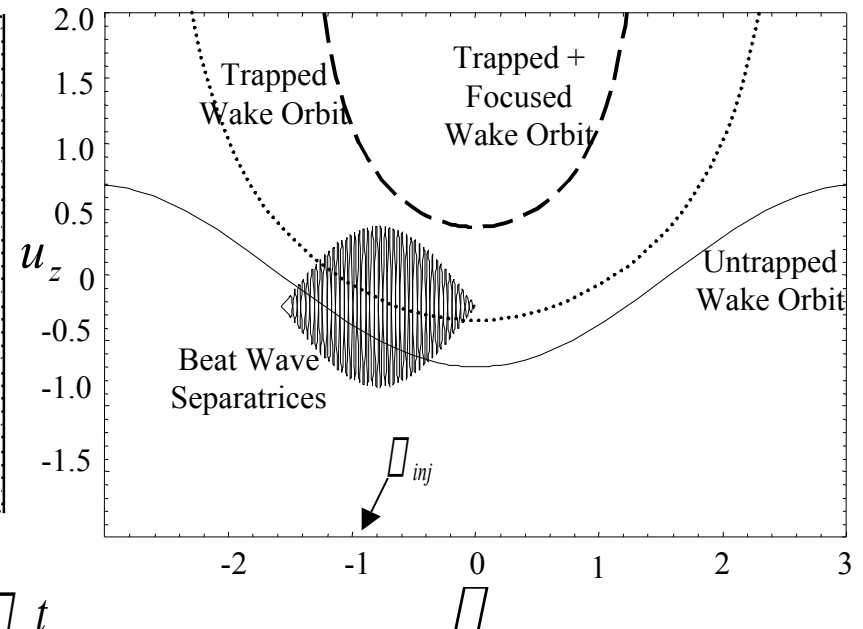
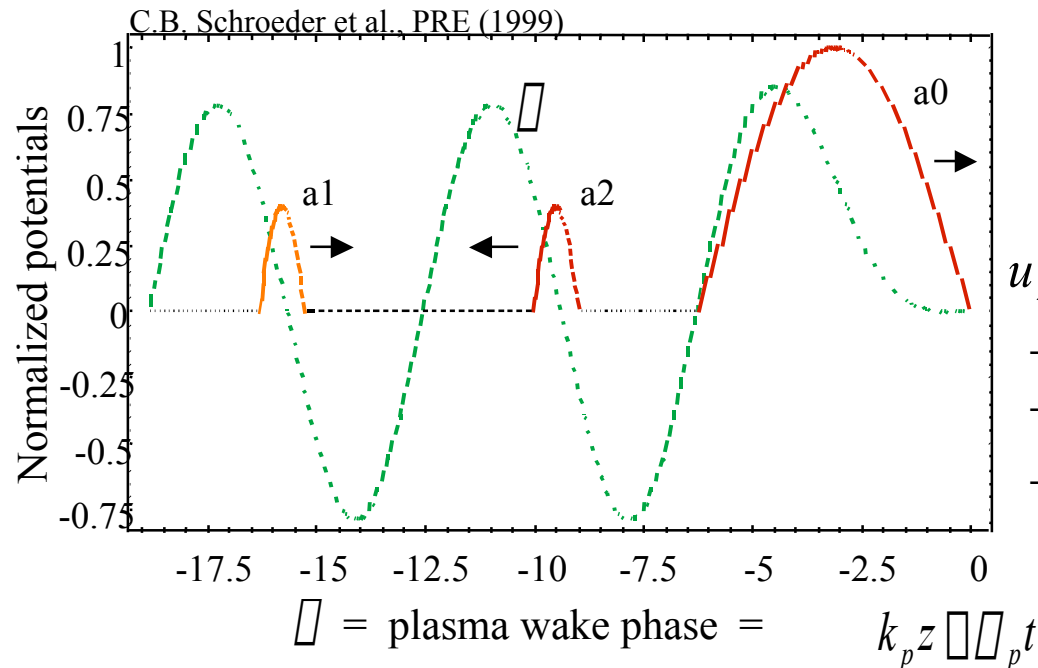






# Generation of Ultrashort Electron Bunches: Colliding Laser Pulse Injection Scheme<sup>†</sup>

<sup>†</sup>E. Esarey *et al.*, PRL, **79**, 2682 (1997)



## Trapping Mechanism:

- I. Pump pulse generates plasma wakefield
- II. Injection pulses collide producing a slow beat wave.
- III. The slow pondermotive beat wave provides untrapped plasma electrons with a phase shift and momentum gain that allows the electrons to be trapped.

## Challenges:

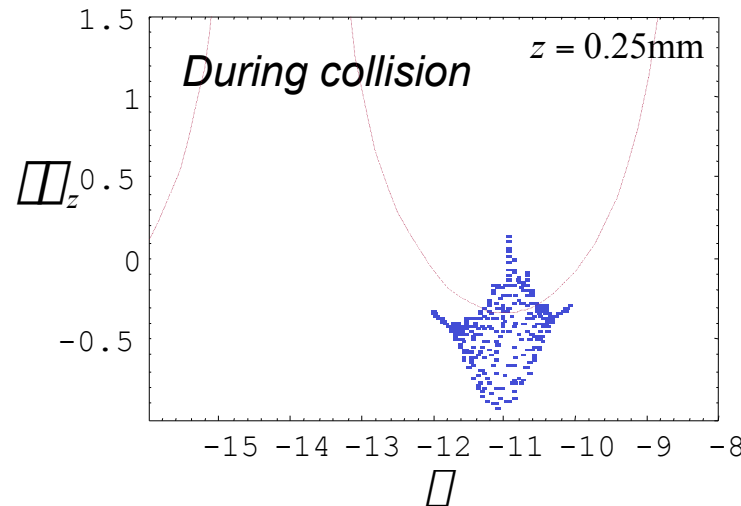
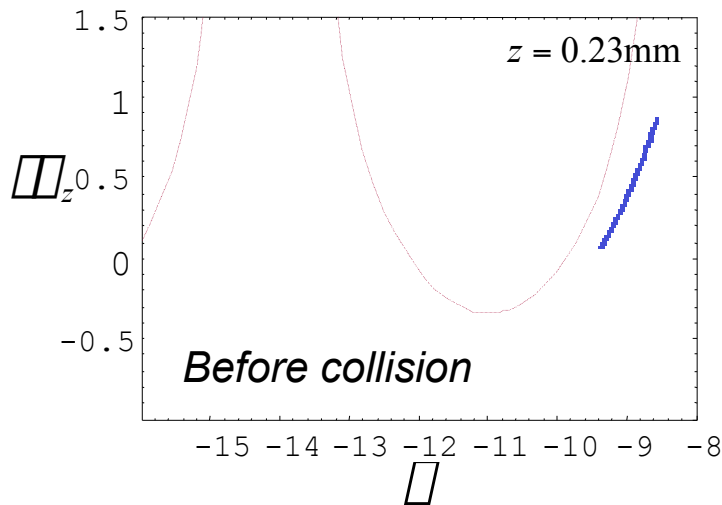
- channel guiding is required (no self guiding)
- timing & pointing of beams

First experiments use tail of a0 as a1 (2 beams)

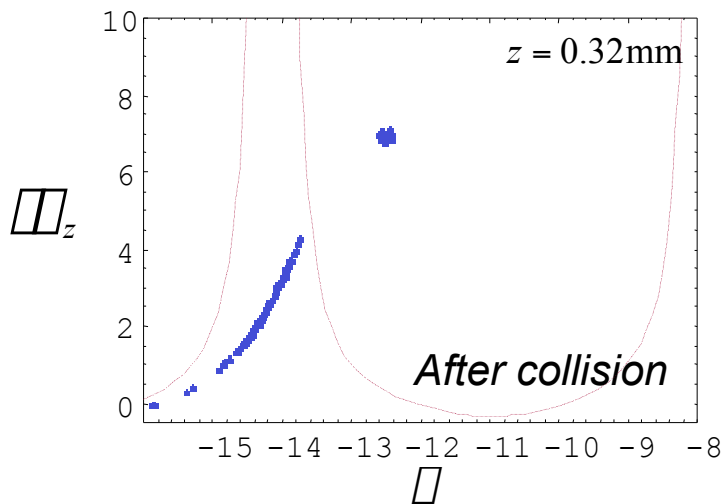


# Simulations of colliding pulse injector show 1 fs, 40MeV beams with < 1% spread

Longitudinal phase space evolution of distribution of plasma electrons



Mean energy = 39 MeV  
Bunch duration = 1 fs  
Energy spread = 0.08 MeV

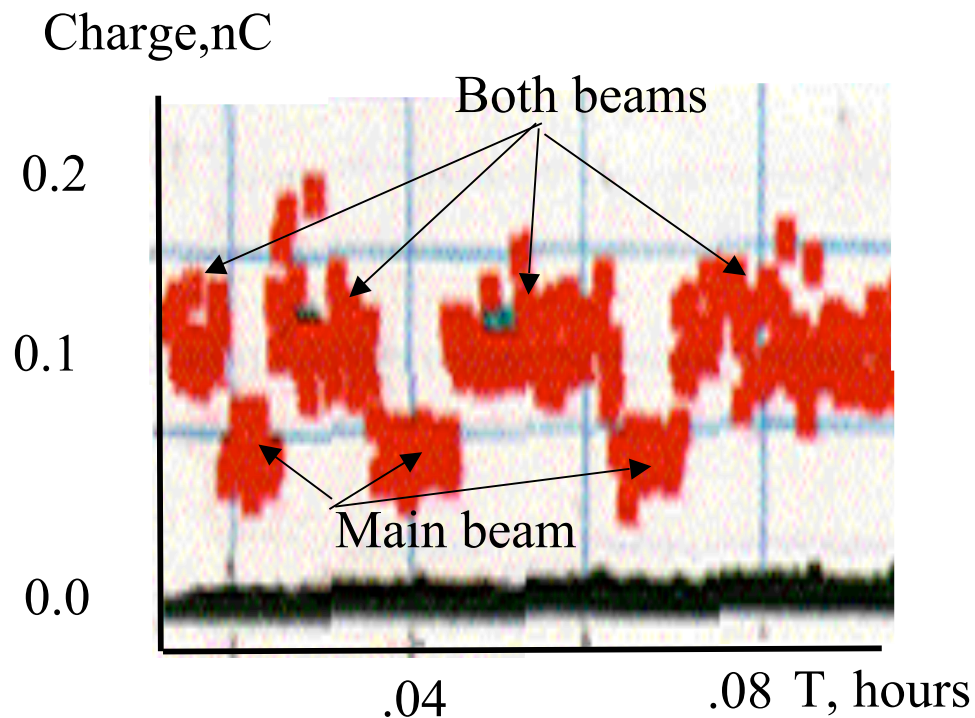


Plasma wavelength	40 $\mu\text{m}$	( $n_0 = 7 \times 10^{17} \text{cm}^{-3}$ )
Pump pulse wavelength	0.8 $\mu\text{m}$	( $\lambda = \lambda_o / \lambda_p = 50$ )
Pump pulse length	40 $\mu\text{m}$	
Pump pulse amplitude	$\sim 0.9$	(wake = $\lambda \sim 0.7$ )
Pump pulse power	5 TW	(spot $\sim 15 \mu\text{m}$ )
Colliding pulse amplitude	$\sim 0.4$	
Colliding pulse length	10 $\mu\text{m}$	
Colliding pulse power	1 TW	
Beat wave phase velocity	-0.2	

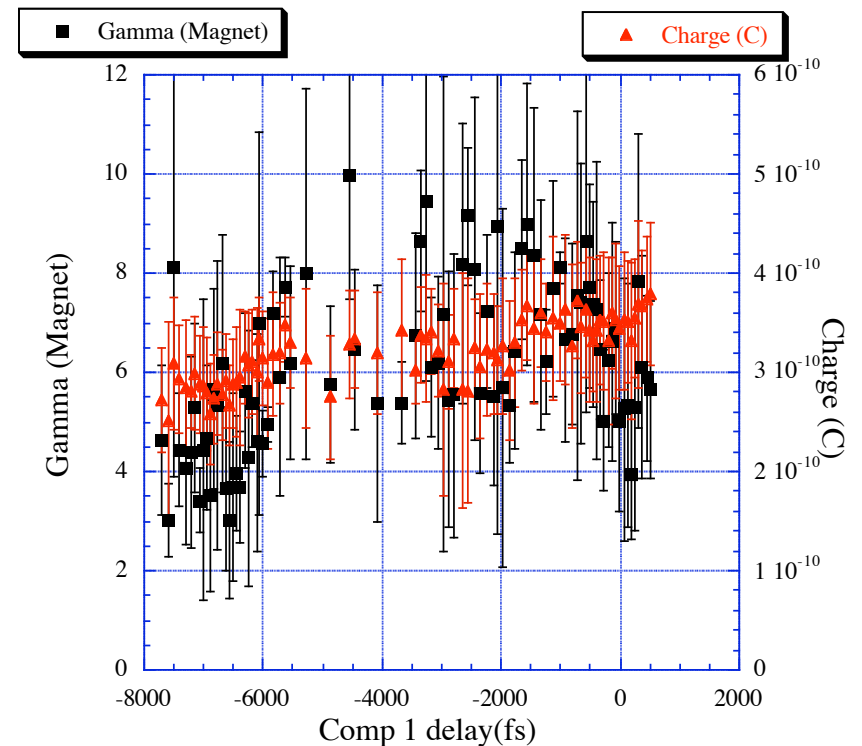


# Colliding pulse experiments have begun

Enhanced electron yield seen  
with 'colliding' beam on



Y and Timing scans do not show  
sensitive dependence  
Further alignment needed





# Experiments are under way

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- Proof of principle experiments are successful
  - Self modulated acceleration
  - Gas jet development
  - Guiding by density channel
- Experimental systems are on line
  - Multi beam interaction chamber
  - Multi arm 10 Hz laser
  - Control, Data acquisition, and timing system
  - Optics in place

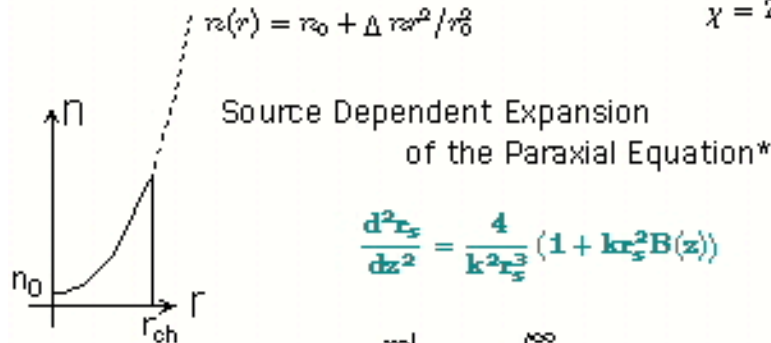
## Work remaining:

- Further characterize and understand self modulated/guided regime
- Demonstrate laser guiding by density channel at high intensities
- Investigate effect of guiding on acceleration (self modulated & standard)
- Injection experiments:
  - Self modulated to channel
  - Colliding pulse

# Laser guiding extends interaction region

$$\hat{E} = \hat{E}_{m,p} L_m^p(\chi) \exp[-(1-i\alpha)\chi/2] \cos(p\theta)$$

$$\chi = 2r^2/r_s^2(z)$$



$$\frac{d^2 r_s}{dz^2} = \frac{4}{k^2 r_s^3} (1 + k r_s^2 B(z))$$

$$B = \frac{m!}{2k(m+p+1)!} \int_0^\infty d\chi k_p^2 \chi^p L_m^p L_{m+1}^p \exp(-\chi)$$

$$B = B_I = -(\Delta n / \Delta n_0) r_s^2 / k r_0^2$$

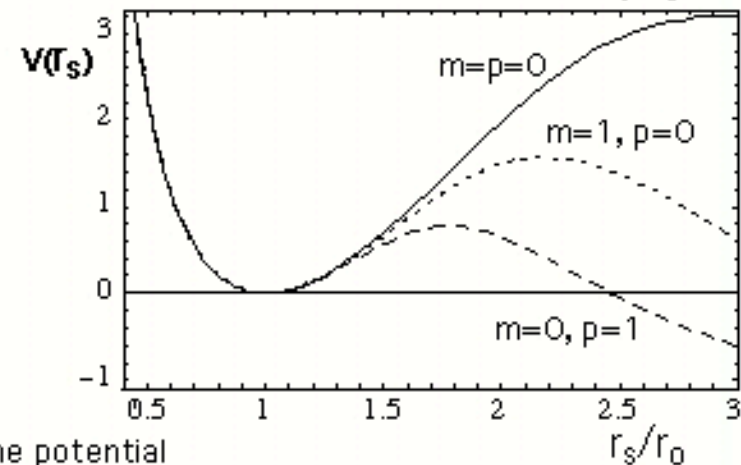
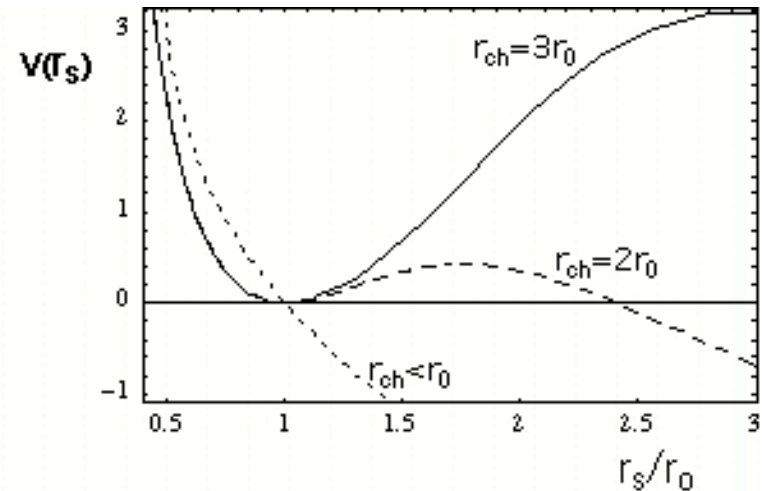
Spotsize evolution is a potential well problem

$$d^2 r_s / dz^2 = -\partial V / \partial r_s$$

$$\partial V / \partial r_s = -4 / k^2 r_s^3 - 4B / k r_s$$

Guiding condition for a beam of  $r_s = r_0 = \text{const}$ : minimum of the potential

$$\Delta n = \Delta n_c = 1 / \pi r_e r_0^2$$

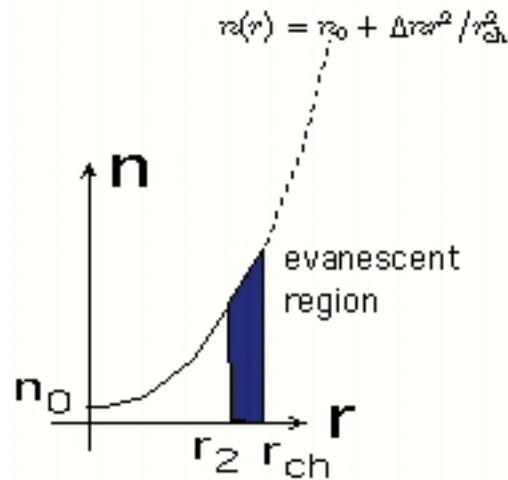


\*E. Esarey, J. Kruel, and P. Sprangle, Phys. Rev. Lett., vol. 72, pp.2887-2890, 1994





# Channel shape determines leakage, higher order mode propagation



For  $p=0$  modes:

$$(\nabla_r^2 + K^2)E=0$$

$$K^2 \sim \omega^2 / c^2 - k_p^2(r) - k_z^2 - p^2 / r^2$$

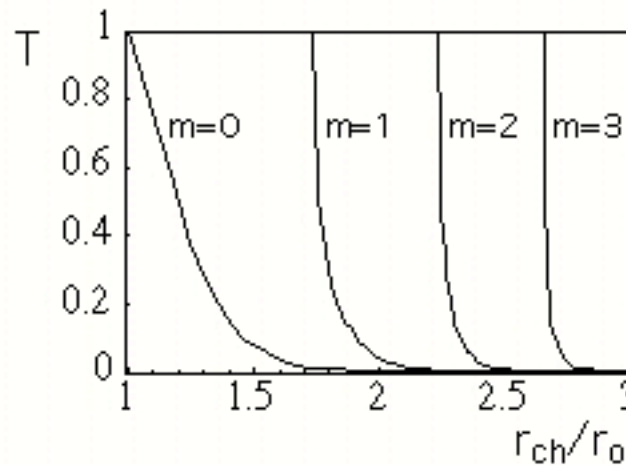
$$k_z^2 \sim \omega^2 / c^2 - k_{p0}^2 - 4(2m + p + 1) / r_0^2$$

Using WKB tunneling theory\*

leakage is  $\exp(-\alpha z)$ , where  $\alpha = T / \Delta Z$  is attenuation coefficient

$$T = \exp \left( -2 \int_{r_2}^{r_{ch}} dr (-K^2)^{1/2} \right)$$

$$\Delta Z = 2k_z \int_{r_1}^{r_2} dr (K^2)^{-1/2}$$



\*P.K. Cheo, *Fiber Optics: Devices and Systems*, (Prentice Hall, Englewood Cliffs - NJ, 1989).



# Trapping of electrons

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Only electrons near the velocity of the wake are accelerated for a long distance.

Low speed electrons only oscillate back and forth in the plasma wave potential but are not trapped.

Need a way to trap electrons:

- A injected beam from a photocathode can be used, but this sacrifices high charge/short pulse advantage of laser driven accelerators.
- High enough wake amplitude traps bulk electrons (wave breaking)
- Raman backscatter wave can give electrons a 'kick' that can allow them to be trapped - but at random phase, leading to 100% energy spread.
- All optical injection methods have been formulated to inject electrons at controlled phase



# I'OASIS 10TW Ti:Al<sub>2</sub>O<sub>3</sub> Chirped Pulse laser for wakefield acceleration

- Electron energy gain proportional to power; 10 TW needed for 1GeV.
- Chirped pulse amplification allows compact high power systems.

